Oscillations MS

1. D

- 2. (a) (Net force) $(\Delta)F=-k(\Delta)x$ (1) Used with F=ma (1)
 - (b) Use of F=(-)kx

Correct answer for k OR substitution of expression for k into formula below (1)

Use of $\omega 2=k/m$ OR T = $2\pi \sqrt{\frac{m}{k}}$ OR $c_{max} = -\omega^2 A$, with $a_{max} = 9.81$ Nkg⁻¹ (1) Use of $\omega = 2\pi f$ OR f=1/T (1) Correct answer for f (1)

Example of calculation:

$$k = \frac{0.15 \text{ kg} \times 9.81 \text{ Nk}^{-1}}{0.2 \text{ m}} = 7.4 \text{ Nm}^{-1}$$
$$\omega = \sqrt{\frac{7.4 \text{ Nm}^{-1}}{0.15 \text{ kg}}} = 7.0 (\text{rad s}^{-1})$$
$$f = \frac{\omega}{2\pi} = \frac{\text{s}^{-1}}{2\pi} = 1.1 \text{ Hz}$$
5

- (b) (i) Any zero velocity point 1
 - (ii) Any maximum/minimum velocity point

[7]

1

1

(c)	Select 70 mm distance from passage/see 35 mm (1)
	Use of $a = -\omega^2 x$ (1)
	Use of $v = \omega A(1)$
	Correct answer (1)

Example of calculation:

$$\omega = \sqrt{\frac{0.89 \text{ms}^{-1}}{3.5 \times 10^{-2} \text{ m}}} = 5.04 \text{rad s}^{-1}$$
$$v = \omega \text{A} = 5.04 \text{s}^{-1} \times 3.5 \times 10^{-2} \text{ m} = 0.18 \text{ ms}^{-1}$$

(d) The answer must be clear and be organised in a logical sequence

The springs/dampers absorb energy (from the bridge) (1)

QWC

(Because) the $\underline{springs}$ deform/oscillate with natural frequency of the bridge (1)

Hence there is an efficient/maximum transfer of energy (1)

Springs/dampers must not return energy to bridge / must dissipate the energy (1) Max 3

[11]

[1]

4

4. B

6. (a) (i) Use of
$$F = -kx (1)$$

 $F = ma (1)$ 2
(ii) cf with $a = -\omega^2 x$ ie $\omega^2 = k/m (1)$
use of $T = 2\pi/\omega$ to result (1) 2
(b) (i) resonance (1) 1
(ii) natural freq = forcing frequency (1) 1

		(iii)	use of $c = f\lambda$ (1) answer 9.1 × 10 ¹³ Hz (1)	2	
		(iv)	use of T = $1/f$ eg T = 1.1×10^{-14} (1) rearrange formula (1) to give 550 N/m(1)	3	[11]
7.	(a)	(i)	Amplitude and frequency 0.17 m (1) 0.8(3) Hz or s ⁻¹ (1)	2	
		(ii)	Maximum velocity Use of $v_{max} = 2\pi f x_0$ (1) Correct answer (1) Example calculation: $v_{max} = 2\pi \times 0.83$ Hz $\times 0.17$ m OR Use of maximum gradient of <i>h</i> versus <i>t</i> graph Answer to 2 sig fig minimum	2	
		(iii)	Velocity-time graph Wave from origin, period 1.2 s (1) Inverted sine wave with scale on velocity axis &initial peak value 0.9 m s^{-1} (1)	2	
	(b)	(i)	Definition of SHM Acceleration / resultant force proportional to displacement OR Acceleration / resultant force proportional to distance from a fixed point [not just distance from equilibrium but ⁻ distance from equilibrium position ⁻ is acceptable] OR $a = (-)$ constant $\times x$ [with a and x defined] OR $F = (-)$ constant $\times x$ [with F and x defined] (1) Acceleration /resultant force directed towards the fixed point / in opposite direction (to displacement) OR negative sign in equation explained [e.g a and x in opposite directions] (1)	2	

(ii) Verifying SHM

8.

		Read off h value and use it to get displacement (1)[only penalise the first mark if h used for displacement throughout]Plot acceleration-displacement graphOR calculate ratios eg $a \div x$ (1)Straight line through the originOR check ratios to see if constant (1)Negative gradient / observe accelerationOR constant is negative (1)			
		OR			
		Use $x = x_0 \cos(2\pi ft)$ for a range of t OR Read off h and get x (1) Use veloce of us and (form part (a)) OB Use $x = (2\pi f^2)$ for range of u (1)	`		
		Use values of x_0 and f from part (a) OR Use $a = -(2\pi f)^2 x$ for range of x (1) Add equilibrium value to x to get h OR Use value of f from part (a) (1) If results agree with values of h (or a) from graph it is SHM (1)	4	[12]	
(a)	• <u>Re</u>	<u>e of effect</u> <u>esonance</u> ea that step frequency = natural frequency of bridge	2		
(b)	(i)	 <u>Why oscillations are forced</u> E.g. amplitude is increasing OR oscillations are driven by the wind 	1		
	(ii)	Calculation of maximum acceleration • Use of $\omega = 2 \pi / T$ to obtain value for ω • Correct answer for acceleration [14 m s ⁻²] Example of calculation: $\omega = 2 \pi / T = 2 \pi / (60 \text{ s} / 38) = 4.0 \text{ s}^{-1}$ $a_{max} = \omega^2 A = (4.0 \text{ s}^{-1})2 \times 0.90 \text{ m} = 14 \text{ m s}^{-2}$	2		
	(iii)	 Show that car loses contact Required a_{max} is greater than g So, at a position (of 0.61 m) above the equilibrium position, vehicle loses contact with the road Example of calculation: 			
		$x = g/\omega^2 = 9.81 \text{ m s}^{-2}/(4 \text{ s}^{-1})^2 = 0.61 \text{ m}$	2	[7]	

9. (a) Experiment

Scheme for timing methods:

QOWC (1) Use f = 1/T OR f = (number of cycles/time taken) (1) Apparatus (1) Principle of method (1) One precaution for accuracy (1)

Max 4

Examples for last three marks:

Stopclock / stopwatch (1) Measure time taken for a number of cycles (1)

ensure vertical oscillations / not exceeding elastic limit (1) Or Motion (OR position) sensor and datalogger (OR computer) (1) Read time for one (or more) cycles from displacement-time graph (1) Read time for several cycles / ensure vertical oscillations (1) Or Light gate and datalogger (OR computer) (1) Computer measures time interval between beam interruptions (1) Use narrow light beam / position gate so beam cut at equilibrium position / ensure vertical oscillations (1) Or Video Camera (1) Read time for one (or more) cycles from video (1) Read time for several cycles / ensure vertical oscillations (1)

[Mark other reasonable techniques on the same principles]

Scheme for strobe method:

QOWC (1) Use stroboscope [Accept strobe] (1) Adjust frequency until mass appears at rest (1) Find highest frequency at which this happens (1) Repeat and average / ensure vertical oscillations (1)

Max 4

Scheme for use of $T m/k / T e/g$	
QOWC (1)	
Calculate T from measured (OR known) m and k using	
T m/k) (1) or calculate T from measured e known g using	
T = e/g(1)	
Use $f = 1/T$ (1)	Max 2
[<i>e</i> is the extension of the spring produced by weight of mass <i>m</i>]	
[Do not give any credit for experiments to measure the resonant	

frequency of the system]

(b)	(i)	<u>Graph</u> Axis labels and single peak (1) Rounded top and concave sides (1) f_0 marked on the frequency axis at, or just to right of, peak. [Amplitude at f_0 should be at least 75% of maximum amplitude] (1)		
		[A sharp kink loses mark 2 only] [Graphs with multiple peaks lose marks 1 and 2; f_0 marked correctly on lowest frequency peak for mark 3] [Ignore whether or not curve goes to origin]	3	
	(ii)	<u>Name of phenomenon</u> Resonance (1) [Mark this independent of whether graph is correct Do not accept "resonant frequency"]	1	
((iii)	<u>Footbridge application</u> People walking / wind / earthquake can cause vibration / act as a driver / apply regular impulses (1) If resonance occurs OR if frequency equals / is close to f_0 we may get large / dangerous / violent oscillations OR large energy transfer OR damage to bridge (1)	2	[10]

10. (a) <u>Diagram</u>

At least 3 crests drawn, with correct even spacing (1) [Judge by eye. Allow +/-20 %. Check in centre of pattern.] Crests approximately straight opposite harbour entrance and curved in the "shadow" region (1) Wavefronts get longer, but diffraction at the edges through no more than 45° (1)

(b) (i) <u>Values from graph</u>

Period: 3.0 (1) [Accept 3] Maximum acceleration: 1.2 [Accept 1.17, 1.18, 1.19, 1.20]

[Both values are needed for the mark. Ignore written units, e.g. "3.0 s", " 1.2 m s^{-2} ".]

(ii) <u>Calculation of amplitude</u>

Use of acceleration = $(-)(2\pi f)^2 x$ (1) Use of f = 1/T (1) Correct answer [0.27 m] (1) [Negative amplitude loses third mark] e.g.

 $\omega = 2\pi / (3.0 \text{ s})$ = 2.09 rad s⁻¹ $A = (1.2 \text{ m s}^{-2}) / (2.09 \text{ rad s}^{-1})^2$ = 0.27 m

(iii) Displacement graph

Cosine curve [Correct way up] (1)		
Axis labelled (i.e. displacement $/ x / y / z$) plus all (1)		
amplitudes consistent with previous answer (i.e. within 1 square)		
plus unit 2 cycles shown with $T = 3$ s (1)	3	
[All zero crossings correct within 1 square]		

[10]

11.	(a)	<u>Meaning of resonance:</u> Parts of building have about the same natural frequency as driving vibrator (1) so vibrate with increased/large amplitude or maximum/large energy transfer occurs (1)		
	(b)	 (i) <u>Why springs reduce vibration:</u> Spring deforms (instead of building) (1) absorbing energy (1) 	2	
		 (ii) <u>Less damage during earthquake:</u> vibration of building is <u>damped</u> / <u>amplitude</u> of vibration is reduced (so damage to building would be less) (1) 	1	[5]
12.	(a)	Time 10 oscillations then divide by 10 / keep eye in the same position each time (1) [do not accept light gates etc]	1	

(b)	Nearest 0.01 m / 1 cm (1) Either suitable because a 1 m length is sensibly measured to nearest 1 cm (1) Or could measure to nearest mm with a metre rule (1)				
(c)	(i)	Column headed $T^2 / 1^{0.5} / \log\log \operatorname{or} \ln\ln (1)$ Units s ² / m ^{0.5} / no units (1) Correct values [T ² check last fig 5.02 / 1 ^{0.5} 0.60 row = 0.78 (1) Log 0.6 row : -0.22 0.210] Scales: points occupy more than half page (1) Points (1) Best fit straight line [not thro origin] (1) [T v l graph marks 4 and 5 only 2 max]	6		
	(ii)	Line does not go through origin (1) Therefore T^2 not proportional to 1 / T not proportional to (1) $l^{1/2}$ (1) [LogLog : Need to find gradient (1) Round off = 0.5]	2 max		
(d)	Line does not go thro origin / When T = 0 there appears to be a value of length (1) Intercept is about cm this shows an error in l (1) The actual length of pendulum is longer than measured (1) The intercept is long enough to be a possible (systematic) error (1) [No marks for log log graphs]				
(e)	Gradient from large triangle (1) = $3.9 - 4.1$ for T ² / = $1.9 - 2.05$ for root 1 (1) Equate with either $4\pi^2/g / 2\pi$ / root g (1) value $9.6 - 10.5$ m s ⁻² (1) [log log intercept (1) = $\log (2\pi / \text{root g})$ (1)(1) value $9.6 - 10.5$ m s ⁻²] (1)		4 max		

[18]

13.	(a)	(a) <u>Definition of SHM</u> Acceleration (OR force) is proportional to displacement/allow distance from point (from a fixed point) / a (OR F) = (–)constant with symbols defined (1) Acceleration (OR force) is in opposite direction to displacement/ Acceleration is towards equilibrium point [Allow "towards a fixe point" if they have said the displacement is measured from this fixed point] / Signs in equation unambiguously correct, e.g. a (OR F) = $-\omega^2 x$		
		motio	ve scheme is the only way to earn 2 marks, but allow 1 mark for on whose period is independent of amplitude OR motion se displacement/time graph is sinusoidal]	2
	(b)	(i)	Calculation of period Use of $T = 2\pi \sqrt{m/k}$ (1) Correct answer [1.1 s] (1) e.g. $T = 2\pi \sqrt{(0.120 \text{ kg} / 3.9 \text{ N m}^{-1})}$ = 1.10 s	2
		(ii)	$\frac{\text{Calculation of maximum speed}}{\text{Use of } v_{\text{max}} = 2 \pi f x_0 \text{ and } f = 1/T \text{ (1)}}$ Correct answer [0.86 m s ⁻¹] (1) e.g. $f = 1/(1.10 \text{ s})$ $= 0.91 \text{ Hz}$ $v_{\text{max}} = 2\pi (0.91 \text{ Hz})(0.15 \text{ m})$ $= 0.86 \text{ m s}^{-1}$	2
		(iii)	Calculation of maximum acceleration Use of $a_{\text{max}} = (-)(2\pi f)^2 x_0$ (1) Correct answer [4.9 ms ⁻²] (1) e.g. $a_{\text{max}} = (2\pi \times 0.91 \text{ Hz})^2 (0.15 \text{ m})$ $= 4.9 \text{ m s}^{-2}$	2
	E.A.	(iv)	Calculation of mass of block Use of T $\alpha \sqrt{m}$ / Use of $T = 2 \text{ km / }\pi (1)$ Correct answer [0.19 kg] (1) e.g. $m = (0.12 \text{ kg})(1.4 \text{ s / }1.1 \text{ s})^2$ = 0.19 kg OR $m = (3.9 \text{ N m}^{-1})(1.4 \text{ s / }2\pi)^2$ = 0.19 kg	2
	[App	ly ecf	throughout]	

[10]

14. (a)	Experimental	verification

(a)	Experimental vermeation		
	QOWC (1) Measure <i>T</i> using clock or motion sensor or video camera or digital (1) camera [Don't accept light gates] for a range of masses (or various masses) (1) Plot <i>T</i> vs m ^{1/2} / Plot T^2 vs <i>m</i> / Plot log <i>T</i> vs log <i>m</i> / calculate <i>T</i> /m ^{1/2} or T^2/m (1)		
	 Str line through origin / Str line through origin / Str line gradient (1) 0.5 / constant One precaution (1) e.g. Use fiducial (or reference) mark Repeat and average No permanent deformation of spring Small amplitude or displacement Measure at least 10T 	Max 5	
(b)	Explanations Natural frequency: Freq of free vibrations / freq of unforced vibrations / freq when it (1) oscillates by itself (or of its own accord) / freq of oscillation if mass is displaced [Don't accept frequency at which it resonates, frequency at which it oscillates naturally, frequency if no external forces]		
	Resonance: When vibration is forced (or driven) at natural frequency (1) Amplitude (or displacement or oscillation) is large (or violent or increases) (1) Amplitude is a maximum / large energy transfer (1) [Accept 4 Hz for natural frequency]	4	[9]
(a)	<u>Definition of longitudinal wave</u> Oscillations OR particles (of medium) move (1) Parallel to <u>direction</u> of wave propagation/travel / energy transfer (1) 2 nd mark consequent on 1 st]	2	
(b)	<u>Collapsing tower</u> Resonance (1) Frequency of quake = natural frequency of tower (1) [Allow resonant frequency for natural frequency]		

15.

16.	(i)	Diagram		
		Component $(mg\cos\theta)$ correctly drawn – good alignment and (1) approximately same length	1	
	(ii)	Diagram		
		Component $(mg\sin\theta)$ correctly drawn, reasonably perpendicular (1) to <i>T</i> to the left	1	
	(iii)	Acceleration		
		Use of $mgsin\theta = ma$ [must see 9.8(1) (m s ⁻²) not 10 for this mark] (1) $a = 0.68 \text{ m s}^{-2}$ [for this mark allow 0.69 m s ⁻² ie 10 m s ⁻² for g] (1)	2	
	(iv)	Direction		
		Directed to O along arc/in same direction as $mg\sin\theta$ /tangential to (1)	1	
		arc		[5]
17.	Grad	ient of graph		
		ient = 2.5 (1)		
		s^{-2} or negative sign (1) uency		
	-	$^2 = 2.5$ [or above value] (1)		
		25 Hz [ecf ONLY for gradient error] (1)	4	
	Perio	<u>id</u>		
	T = 4	s ecf their $f(1)$	1	
	Acce	leration against time graph		
	Any	sinusoidal curve over at least two cycles (1)		
	Nega	tive sine curve (1)		
		s scale showing $a = 20 \text{ (mm s}^{-2}) \text{ OR } x$ axis scale showing $4(s) / \text{ their } T$	3	
			-	[8]
10	C.			
18.		litions for simple harmonic motion		
		leration OR restoring force \propto displacement (1)	2	
	-	posite direction / towards equilibrium position (1) child's motion only approximately simple harmonic	2	
	-	one from:		
	•	amped / friction opposes motion / air resistance		
		ving's path is arc of circle, not straight line		
		ngle too large (1)	1	
	• al		1	

Calculations

(i) Period of the motion: T = 20 s/6 = 3.3 s (1) f = 1/T = 0.30 Hz (allow e.c.f. for *T*) (1)

- (ii) Value of ω Use of $\omega = 2\pi f$ $= 2\pi \times 0.30$ = 1.9 rad s⁻¹ (allow e.c.f. for *f*, no repeat unit error) (1)
- (iii) Child's acceleration:

 $a_{\text{max}} = -\omega^2 A$ (1) = $-1.9^2 \times 1.2$ (allow e.c.f for ω) (1) = (-) 4.3 ms⁻²

Swing an example of resonance

Push (driver) at same frequency as swing (driven) (1)		
causes increase of amplitude / energy transfer (1)	2	

[10]

2

3

19. <u>Simple harmonic motion</u>

Acceleration proportional to displacement (from equilibrium position/ point) (1)	
and in opposite direction/directed towards equilibrium position / point) (1)	

OR accept fully defined equation

Oscillations

 $x_0 = 0.036 \text{ m}$ (1)

Period = 7.60 s/20 = 0.380 s (1) f = 2.63 Hz (1)

Displacement when t = 1.00 sx = (-)0.026 m (1)1How and why motion differs from prediction1Motion is damped/amplitude decreases with time (1)
(Because of) air resistance (1)2[8]

20.	Oscillating, system		
	Diagram: suitable oscillator (1) method of applying periodic force of variable frequency (1)	2	
	Natural frequency:		
	(With no periodic force) displace oscillator and let it oscillate (freely) (1)		
	Frequency of this motion is natural frequency (1)		
	Forced oscillation:		
	Their system is being forced to oscillate/vibrate at driver's frequency (1)		
	Resonance:		
	Vary the frequency (1)		
	Oscillator has large amplitude at / near natural frequency (1)	5	

[7]

21.	(a)	(i)	<i>a</i> is acceleration				1
			f is frequency				1
			x is displacement from	om equilibrium/ce	ntre/mean posit	ion	1
			[beware amplitude]				
			Either minus sign m centre/equilibrium p OR <i>a</i> and <i>x</i> in oppos	osition/mean posi	tion	lacement	1
					spposite to disp		1
		(ii)	Attempt to use $v_m =$	$2\pi fa$			1
			$v_{\rm m} = 2\pi(50 \text{ Hz}) (8.0$	$v_{\rm m} = 2\pi (50 \text{ Hz}) (8.0 \times 10^{-6} \text{ m}) [a = 4 \times 10^{-6} \text{ m e.o.p}]$			
			$= 2.5 \times 10^{-3} \text{ m s}^{-1}/2$	2.5 mm s ⁻¹ /2500 μ	um s ⁻¹		1
	(b)	(i)	$ ho$ in kg m $^{-3}$ and g in	-			1
			$A \rho g/m$ with units lea	$A \rho g/m$ with units leading to s ⁻²			1
		(ii)	At least three peaks	of <i>y/m</i> measured [ignore numbers	5]	1
			EITHER				
			(5.4/5/6 1.2	3.7/6/8	2.4	1.6/7	
			4.4	2.8/9	2.0/1.9	1.4)	
			Attempt to calculate Logical statement re			5]	1 1

	OR Read 3 values of x and y [ignore numbers] Two half lives between 0.75 s and 0.95 s Logical statement re half-lives and exponential change [beware Δy not constant / use of $y = Y_0 e^{-kt}$]	1 1 1	[12]
22.	Simple harmonic motion – conditions		
	Acceleration (or force) proportional to displacement [OR $a \propto -x$] (1)		
	Acceleration (or force) directed towards equilibrium position (1)	2	
	<u>Graph</u>		
	Horizontal line at $E_p = 19 \text{ J} (1)$	1	
	Calculations		
	(i) Use of $E_K = E_r - E_p$ (1) = 19J - 5J = 14 J (1)		
	(ii) Use of $Ep = \frac{1}{2} kx^2$ (1) with readings from graph (1) e.g. $k = 2 \times 5 \text{ J} / (0.02 \text{ m})^2 = 2.5 \times \text{N m}^{-1}$ (1)		[8]
23.	Simple harmonic motion		
	Acceleration/force is proportional to <i>displacement</i> (1)	_	
	but in the opposite direction / towards equilibrium point /mean point (1)	2	
	<u>Graph</u>		
	Sine curve (1)		
	-ve [consequent] (1)		
	A and B / (i) and (ii) / $a \& x$ [beware $a \lor x$] (1)	3	[5]

	Equation for shm: $x = A \cos \omega t$		
	A amplitude = $1.0 \text{ mm or } 1.0 \times 10^{-3} \text{ m}$		
	$\omega = 2\pi f = 6.28 \times 10^2 \text{ (rad s}^{-1)} - \text{no unit penalty for } \omega \text{ (1)}$	2	
	Calculations		
	(i) $A = A \omega^2$		
	= 1.0×10^{-3} m × (6.28×10^{2} rad s ⁻¹) ² = 394 m s ⁻² (1)		
	(ii) $\upsilon = A \omega$ (1)		
	= 1.0×10^{-3} m × 6.28×10^{2} rad s ⁻¹ = 0.63 m s ⁻¹ (1)	3	
	Acceleration - time graph		
	Two cycles of sinusoidally shaped graph (1)		
	Period = 10 m s (1)		
	Amplitude = 394 m s^{-2} [e.c.f from (i)] (1)	3	
	Explanation		
	Resonance (stated or implied by explanation) (1)		
	Increased amplitude at resonant frequency (1)	2	[10]
25.	Simple harmonic motion Force/Acceleration proportional to displacement/ $a = \omega^2 x$ (1) [define a and x but not ω]		
	In opposite direction to displacement/ towards a fixed point/towards equilibrium position/minus sign (1)	2	
	Oscillation of massClarity of written communication (1)Down: $T > W$ [W varying 0/3] (1)Up: $T < W$ (1)		
	T > W gives resultant force/acceleration UP (1) [or equivalent argument for displaced up]	4	

<u>Velocity-time graph</u> Either Cosine graph [zigzag -1 here] (1) Starting at positive maximum [if very poorly synchronised 0/2] (1)

24. Data for speaker and equation

	<u>Maximum velocity of mass</u> Period = 0.50 or amplitude = 0.07 (1) Use of $f = I/T$ / Use of $x = x_0 \sin \operatorname{or} \cos(\omega t)$ (1) Use of $v_{\text{max}} = 2\pi f x_0$ (1) 0.88 m s ⁻¹ (1)		
	OR v_{max} = gradient at 0.50 s (or equivalent) (1) Correct method for gradient (1) Answer in range 0.8 to 1.0 m s ⁻¹ (1) [Max 3 for gradient method]	4	[12]
26.	Simple harmonic Acceleration (OR force) \propto displacement (1)		
	and in opposite direction (1)		
	[OR $F = -kx$ (1) OR $x = A \cos \omega t$ (1) symbols defined (1)]	2	
	Graph(i) E_k inverse of potential energy curve(ii) T horizontal line at 2×10^{-6} JStiffnessUse of $E = \frac{1}{2} kx^2$ (1) $2 \times 10^{-6} = \frac{1}{2} k 0.10^2$ $k = 4 \times 10^{-4}$ J m ⁻² (1)[accept N m ⁻¹]	2	
	Variation in potential energyAny 3 points from the following:• $I_{150}/I_{100} = 100^2/150^2 = 0.44$ • So $E_{max} = 0.44 \times 2 \times 10^{-6} = 0.88 \times 10^{-6}$ (J) [no u.e]• Curve through (0,0), max $0.8 - 0.9$ • Curve the same		
	• $I \propto (\text{amplitude})^2$	Max 3	[0]

27. Frequency:

Natural frequency/fundamental frequency (1) [Not resonant]

Explanation:

Resonance occurs when driving frequency = natural frequency (1)	
causing maximum energy <u>transfer(1)</u>	
increased/maximum amplitude (1)	Max 2

Graph:

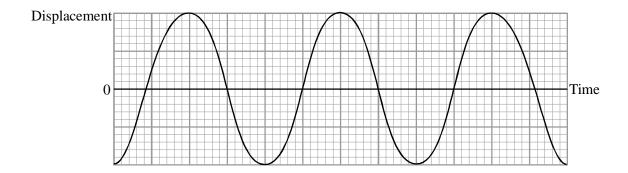
Undamped - marked A	
Acceptable shape - narrow peak (1)	
Resonant frequency marked under graph max. (1)	
Damped - marked B	
B - entire graph below A (1)	
[Accept touching graphs] (1)	4
Peak covers greater frequency range than A	

Prevention of resonance:

Damps oscillations (1)Fewer forced oscillations (1)Explanation of damping [e.g. in terms of energy transfers] (1)Max 2

28. Displacement-time graph:

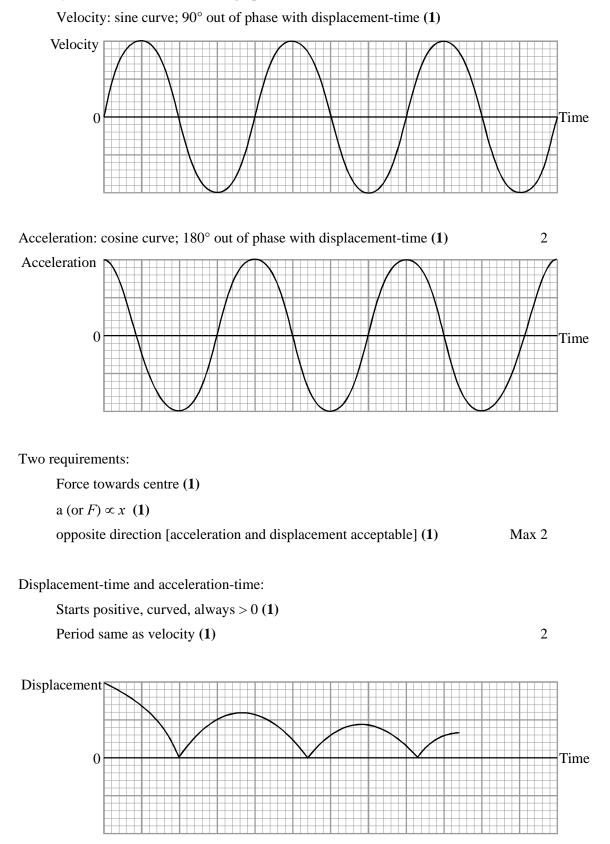
Cosine curve (1) Constant period and amplitude (1)



[9]

2

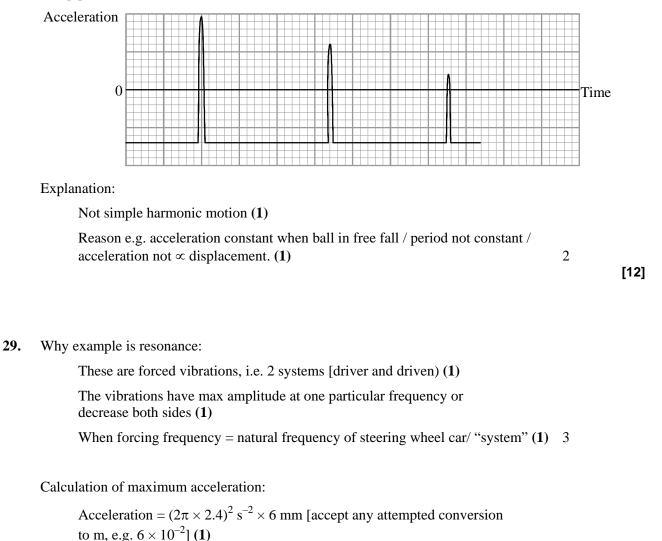
Velocity-time and acceleration-time graphs:



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Acceleration constant not equal to 0(1)

Sharp peak when ball in contact with floor (1)



= 1400 (1360) mm s⁻² [no e.c.f.] (1) (1.4 m s⁻²)

[5]

2

30.	A body oscillates with simple harmonic motion when the resultant force <i>F</i> acting on it and its displacement <i>x</i> are related by the expression		
	$F = -kx \text{ or } F \propto -x.$		
	The acceleration of such a body is always directed towards the centre of the oscillation or in the opposite direction to displacement/x =		
	0 /equilibrium/similar		
	The acceleration of the body is a maximum when its displacement is		
	maximum and its velocity is maximum when its displacement is zero.	4	
	Force constant:		
	= 14 N m ⁻¹ or kg s ⁻²	2	
			[6]
31.	Displacement-time graph:		
	Sine or cosine (1)		
	Max/min at $+1.8$ and -1.8 (1)		
	T = 0.05 s and at least one cycle (1)	3	
	Calculation of maximum speed:		
	Correct <i>use</i> of $v = ax_0 \text{ or } 2\pi f x_0$		
	$= 2\pi \times 10 \text{ s}^{-1} \times 1.8 \times 10^{-2} \text{ m} \textbf{(1)}$		
	Maximum speed = 2.3 m s^{-1} (226 cm s ⁻¹) (1)	2	
	Any two places correctly marked M (1)	1 [Total 6 mar	ks]

32. A student was studying the motion of a simple pendulum the time period of which was given by $T = 2\pi (l/g)^{\frac{1}{2}}$.

He measured T for values of l given by

$$l/m = 0.10, 0.40, 0.70, 0.70, 1.00$$

and plotted a graph of T against \sqrt{l} in order to deduce a value for g, the free-fall acceleration. Explain why these values for l are poorly chosen.

An inadequacy PLUS a reason why (many possibilities) e.g. some values too short to produce accurate T values; when the values are square rooted; spacing is unsatisfactory. (1)

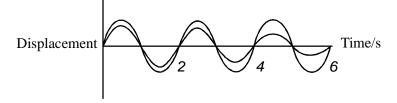
(1 mark)

How would the student obtain a value of g from the gradient of the graph?

Gradient =
$$\frac{2\pi}{\sqrt{g}}$$
 (1)
Hence $g = \frac{4\pi^2}{(gradient)^2}$ (1)

(2 marks)

The graph below shows three cycles of oscillation for an undamped pendulum of length 1.00 m.

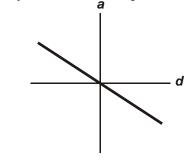


Add magnitudes to the time axis and on the same axes show three cycles for the same pendulum when its motion is lightly air damped.

T = 2 s (1) $T_{\text{damped}} = T_{\text{original}}$ (1) Amplitude reduced (1) Continuous reduction in amplitude (1)

> (4 marks) [Total 7 marks]

33. A body oscillates with simple harmonic motion. On the axes below sketch a graph to show how the acceleration of the body varies with its displacement.



Straight line through origin (1) Negative gradient (1)

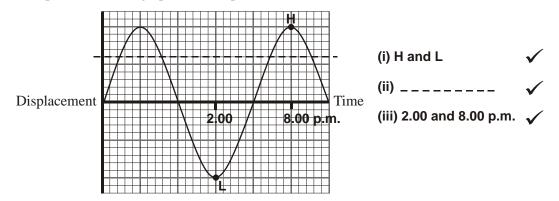
(2 marks)

How could the graph be used to determine T, the period of oscillation of the body? **Reference to gradient of line** (1)

Gradient = (-)
$$\omega^2 \underline{\text{or}} = (-)(2\pi f)^2$$

OR $T = \frac{2\pi}{\sqrt{(-)gradient}}$ (1)
(2 marks)

A displacement-time graph from simple harmonic motion is drawn below.



The movement of tides can be regarded as simple harmonic, with a period of approximately 12 hours.

On a uniformly sloping beach, the distance along the sand between the high water mark and the low water mark is 50 m. A family builds a sand castle 10 m below the high water mark while the tide is on its way out. Low tide is at 2.00 p.m.

On the graph

- (i) label points L and H, showing the displacements at low tide and next high tide,
- (ii) draw a line parallel to the time axis showing the location of the sand castle,
- (iii) add the times of low and high tide.

(3 marks)

Calculate the time at which the rising tide reaches the sand castle.

Use of $x = x \sin \omega t$ $15 = 25 \sin \omega t$ $\omega = \frac{\pi}{6}$ or $\omega t = 37^{\circ} / t = 1.23$ hours Time = 6.14 p.m. ANY THREE LINES (3) Full error carried forward from wrong diagram Alternative using graph: Identify coordinates (1) Convert to time (1) Add to reference time (1)

(3 marks) [Total 10 marks]